

# An All Sky Cirrus Confusion Noise Map for WIRE

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## 1. WIRE Requirements

The Wide Field Infrared Explorer (WIRE) is an infrared space observatory being developed under NASA's small explorer program for launch in late 1998 (Schember, et al, 1996). WIRE's main function will be to produce a sky survey at wavelengths of 12 and 25  $\mu\text{m}$  covering several tens of square degrees at a sensitivity of 0.2 mJy,  $5\sigma$  at 25  $\mu\text{m}$ , and several hundred square degrees at a sensitivity of 0.7 mJy,  $5\sigma$  at 25  $\mu\text{m}$  to study starburst galaxies and search for luminous protogalaxies. The exact sensitivity requirements depend on the, as yet unknown, evolutionary history of very distant galaxies. The numbers above represent the worst case for sensitivity requirements, that is no evolution. WIRE will use a 30 cm telescope and 128x128 Si:As array detectors with  $0.5^\circ \times 0.5^\circ$  fields of view to produce the survey.

The high sensitivity levels needed for WIRE science cannot be achieved every where over the sky due to background confusion from galactic sources. WIRE need not attempt survey observations at low galactic latitudes where many sources of intense emission contribute to the background confusion. At higher latitudes where WIRE must operate, background confusion from dust emission, the infrared cirrus, remains and must be evaluated to provide a criterion for selection of suitable WIRE survey areas. WIRE science requires confusion noise levels below 10% of the  $5\sigma$  sensitivity levels at 25 mm:  $< 23 \text{ mJy}, 1\sigma$  for the deep survey and  $< 115 \text{ mJy}, 1\sigma$  for the moderate survey.

## 2. Method

Gautier, et al. (1992) presented a method for predicting noise in point source flux measurements due to background fluctuations which uses the spatial power spectral distribution (*PSD*) of the background. Given a particular geometry and scale of signal and background apertures on the sky, the expected fluctuation in [*source flux* = (*signal* + *background*) - *background*] can be related to the *PSD* of the background. For power law *PSDs* ( $PSD = P_0 d^{-\alpha}$ , see below) the rms fluctuation is

$$\text{rms} = \sqrt{PSD(d_0) E_0} (d/d_0)^{(1+\alpha/2)} \quad (1)$$

where  $\alpha$  is the power law index of the *PSD*,  $d$  is the scale of the aperture geometry,  $d_0$  is a normalizing scale and  $E_0$  is a constant associated with  $d_0$  and the geometry of the apertures. This technique can be used to predict the confusion noise contribution to WIRE measurements if the *PSD* of the 25  $\mu\text{m}$

cirrus **emission** can be determined **at** the spatial scales relevant **to** WIRE. The IRAS ISSA all sky map data provides a basis for measurement of cirrus *PSD* over large regions **of** the **sky**.

Gautier, et al. (1992) and Abergel, et al. (1996) have measured the *PSD* of infrared cirrus emission seen in the IRAS data at 12, 25, 60 and 100  $\mu\text{m}$  and have found it to be well represented by a power **law**. Cutri (Low and Cutri, 1994) has performed a similar analysis on the visible red light from reflection nebulae associated IRAS cirrus clouds and also found power law *PSDs* with indices essentially equal to those seen in the infrared. These observations suggest that **it is** reasonable to predict the *PSD* of 25  $\mu\text{m}$  cirrus **at** WIRE spatial scales by measuring the *PSD* of cirrus **at** 100  $\mu\text{m}$  on spatial **scales** accessible **in** the IRAS **data**, extrapolating **to** WIRE scales and correcting with the observed 25  $\mu\text{m}$ /100  $\mu\text{m}$  flux **ratios**. IRAS ISSA data supplies *PSD* information **at** scales near  $1^\circ$ . Extrapolation by a factor of about 120 is needed **to** reach the WIRE point source extractor scale. Data and arguments presented **in** the next section indicate that the uncertainty in the WIRE noise prediction **is** about **a factor of 2** for this extrapolation. Fluctuations in the 25  $\mu\text{m}$ /100  $\mu\text{m}$  flux ratio on the order of **a factor 3** may occur. These factors should result in an uncertainty **of** about **a factor of 4** in the WIRE noise prediction; useable **for** survey planning. Monitoring **of** the 25  $\mu\text{m}$ /100  $\mu\text{m}$  flux ratio, at least at lower galactic latitudes where the 25  $\mu\text{m}$  flux **is** available, can improve this uncertainty.

The Fourier transform method for determination **of** sky background *PSDs* used by Gautier, et al. (1992) **does not** lend **itself** to good spatial resolution **in** determination **of** the *PSD* because the Fourier transform smears spatial information **at** all scales over the whole transform space. The WIRE survey planning needs spatial **resolution** on the degree scale for its cirrus noise predictor. Wavelet transforms **use** basis functions of finite extent and **offer** a method for obtaining spatially resolved *PSD* information (Farge 1992). The noise predictor described here uses a Burt pyramid wavelet transform technique **which** convolves images with a series **of** low pass filters and combines the results **to** effectively produce ISSA maps filtered with **a** series of constant **Q** band pass **filters** spaced **every octave**. The wavelet filter pass bands were calibrated for gain and effective scale using synthetic maps with known power law  **$P(f)$** s. The mean square value, averaged **over** an area several times the **size** of the wavelet kernel, of a calibrated, filtered image effectively reproduces the Fourier transform power **law** spectrum sampled **every octave** and allows good determination of the index and value of the *PSD*. Higher spatial resolution than the  $12.5^\circ \times 12.5^\circ$  of the ISSA map is obtained by averaging the wavelet filtered images over smaller blocks **of** the image. **A** conceptually similar method was used by Abergel, et al. (1996).

### 3. Results

Wavelet *PSD* analysis has been used to predict the cirrus confusion noise for WIRE in eight  $12.5^\circ \times 12.5^\circ$  ISSA fields with galactic latitude ranging from  $11^\circ$  to  $50^\circ$  (Table 1). The ISSA 100  $\mu\text{m}$  maps were first cleaned of bright compact sources, filled out to  $512 \times 512$  pixels by removing the average value of the map and tapering the edge to zero over six pixels and given a mild treble boost to remove most of the ISSA transfer function as determined from an average of

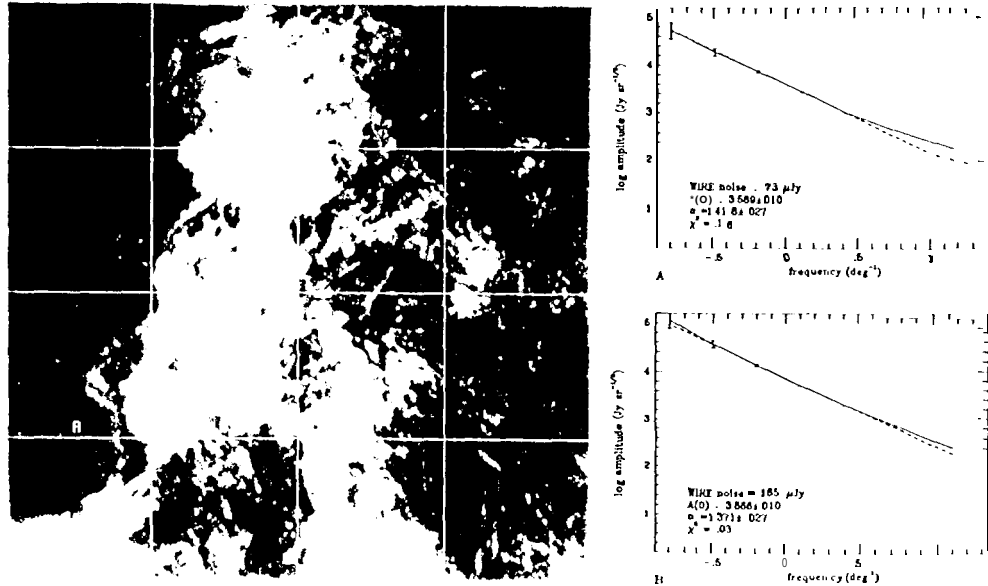


Figure 1. Left) ISSA field 430, after removal of point sources and anodization. The grid divides the image into the averaging regions for the wavelet PSD spectra. Right) Wavelet PSD spectra for the two grid arms indicated. The calculated values of  $\chi^2$  are suspect since they include only formal uncertainty estimates of the wavelet filter process and not any estimate of variation of the real cirrus structure distribution.

point spread functions found in the ISSA maps. Next a double density Burt pyramid wavelet transform using a separable 5x5 filter kernel was applied to produce seven output maps corresponding to scales from about 3' to 3°. The rms value of the transform maps was produced by averaging over sixteen 3"x3" blocks corresponding to 128x128 pixels of the original map. This averaging is sufficiently large to be useful for all but the largest scale transform map where only sixteen output pixels are averaged. Figure 1 shows the wavelet PSD spectra and predicted WIRE noise in this 4x4 grid of 3°x30' arms for two ISSA fields. The power law fit excluded the largest scale and the two smallest scales. As explained above, the largest scale was excluded because of insufficient averaging, the smallest two scales are adversely affected by the treble boost function derived from the ISSA point sources.

The WIRE flux extractor is assumed to have an annular geometry with a source aperture of 29.6" diameter surrounded by a background ring of 29.6" width. The 100  $\mu$ m/25  $\mu$ m brightness ratio for cirrus was assumed to be 15.54  $\pm$  30% for conversion from 100  $\mu$ m PSD to 25  $\mu$ m PSD value (Gautier and Stewart, 1994 and Boulanger and Perault, 1988).

The expected uncertainty of the WIRE noise prediction has been estimated from the calibration of the wavelet pass band filters and the quality of the fit of the observed PSD to a power law. The 10 error bars shown in Figure 1 are derived from the distribution of wavelet power obtained from analysis of synthetic

Table 1. Regions analyzed.

Area	ISSA Field	R.A.	Dec.	$l$	$b$
Chamaeleon	006	12h. 00m	-80	300.8	-17.6
Taurus	276	4h. 12m	+20	174.6	-21.7
Taurus	277	4h. 54m	+20	181.2	-14.1
Taurus	311	4h. 36m	+30	170.6	-11.0
Taurus	413	8h. 40m	+70	139.0	+42.6
Ursa Major	414	10h. 24m	+70	139.0	+42.6
Ursa Major	430	0h. 00m	+90	123.0	+27.4
North Polar Cloud		10h. 27m	+58	151.8	+50.5
III hole					

images with well defined power law spectra. Additions to the uncertainty from statistically expected departures of the cirrus structure from an exact power law have not yet been made. A preliminary estimate of the uncertainty added by the natural cirrus indicates that the error for the small scale wavelet power should be that of the point at  $\log f = -0.2$ . Then the  $1\sigma$  uncertainty on  $\alpha$  increases to  $\approx 0.043$ . This results in a  $3\sigma$  factor of  $120^{(129)} = 1.85$  uncertainty, from this source, in the predicted WIRF noise. The estimate of a factor of 2 uncertainty in the WIRF noise due to  $PSD$  estimation given above seems reasonable.

#### 4. Current Work

We are in the process of extending the WIRF noise predictions to all of the sky above about  $|b| > 10$  and increasing the spatial resolution to  $< 2^\circ$ . The ultimate goal is to produce an all sky ( $|b| > 10$ ) noise prediction map for use with the WIRF survey scheduling tool. The next need is to understand how much the usable deep and moderate survey sky exceeds our previous expectations and what effect this will have on WIRF observing efficiency. We are also investigating the efficiency of other confusion noise predictors, such as the shape of image histograms, which can be derived from the ISSA data more easily than the  $PSD$  function. Other such predictors would be calibrated with the  $PSD$  method.

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